

Flavour independent search for Higgs bosons decaying into hadronic final states in e^+e^- collisions at LEP

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Abstract

A search for the Higgsstrahlung process $e^+e^- \rightarrow hZ$ is described, where the neutral Higgs boson h is assumed to decay into hadronic final states. In order to be sensitive to a broad range of models, the search is performed independent of the flavour content of the Higgs boson decay. The analysis is based on e^+e^- collision data collected by the OPAL detector at energies between 192 and 209 GeV. The search does not reveal any significant excess over the Standard Model background prediction. Results are combined with previous searches at energies around 91 and at 189 GeV. A limit is set on the product of the cross-section and the hadronic branching ratio of the Higgs boson, as a function of the Higgs boson mass. Assuming the hZ coupling predicted by the Standard Model, and a Higgs boson decaying only into hadronic final states, a lower bound of $104 \text{ GeV}/c^2$ is set on the mass at the 95% confidence level.

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1. Introduction

In the Standard Model (SM) and for masses relevant to the LEP energy range, the Higgs boson is predicted to be produced principally by the Hig-

gsstrahlung process $e^+e^- \rightarrow hZ$ and to decay dominantly into the $b\bar{b}$ channel. This is also the case in large domains of the Minimal Supersymmetric Standard Model (MSSM) parameter space (the Higgs phenomenology is reviewed, e.g., in Ref. [1]). Most of the

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searches conducted so far at LEP, therefore, tag the b flavour to enhance the Higgs boson signal.

In other scenarios, however, the decay of the Higgs boson into lighter quark flavours or into gluon pairs may be important. Such is the case in general models with two Higgs field doublets (2HDM) [1,2] or other extended models [3]. In order to be sensitive to Higgs bosons predicted by such models, the search described here is based only on kinematic selections which are insensitive to the hadron flavour present in the final state. Such searches have already been reported by OPAL; these were based on data collected at energies close to the Z boson resonance [4] and at a centre-of-mass energy (\sqrt{s}) of 189 GeV [5]. A similar search has also been reported by ALEPH [6].

This Letter describes a flavour independent search which is based on OPAL data collected at centre-of-mass energies between 192 and 209 GeV with an integrated luminosity of about 420 pb^{-1} . For the results presented, this search is combined with the earlier OPAL searches [4,5].

2. Data sets and Monte Carlo simulation

The OPAL detector is described in Ref. [7]. The events selected for the analysis have to satisfy a set of detector status requirements which ensure that all relevant detector elements are active. Events are reconstructed from charged particle tracks observed in the central tracking detector and energy deposits (“clusters”) in the electromagnetic and hadron calorimeters. The tracks and clusters are required to pass a set of quality requirements [8]. In calculating the visible energies and momenta E_{vis} and \vec{P}_{vis} , either for individual jets or for the events, corrections are applied to prevent double-counting of the energy attributed to the tracks and to the clusters geometrically associated to the tracks [9].

The data sets to which the present analysis applies were collected in 1999 at \sqrt{s} between 192 and 202 GeV and in the year 2000 at \sqrt{s} between 200 and 209 GeV. After the detector status requirements the data sample has an integrated luminosity of approximately 420 pb^{-1} . The exact amount varies among the different channels (see Table 1).

A variety of Monte Carlo samples have been generated to estimate the selection efficiencies for the Higgs

boson signal and for the background processes. In order to cover the range of energies of the data, the simulations are performed at fixed values of \sqrt{s} between 192 and 210 GeV and for a set of Higgs boson masses. Spline fits are used to calculate the signal efficiencies at intermediate values.

The Higgsstrahlung process is modelled with the HZHA generator [10]. Samples of 1000 to 5000 events were produced at fixed masses, between 30 and $120 \text{ GeV}/c^2$. The Higgs boson is required to decay, either according to the SM, or separately to $c\bar{c}$, $s\bar{s}$ or to pairs of gluons.

The simulated background samples typically have more than 30 times the statistics of the collected data. The following event generators are used: KK2F [11] and PYTHIA [12] for the process $q\bar{q}(\gamma)$, grc4f [13], KORALW [14] and EXCALIBUR [15] for the four-fermion processes, BHWIDE [16] for $e^+e^-(\gamma)$, KORALZ [17] for $\mu^+\mu^-(\gamma)$ and $\tau^+\tau^-(\gamma)$, and PHOJET [18], HERWIG [19] and VERMASEREN [20] for hadronic and leptonic two-photon processes and for $e^+e^- \rightarrow e^+e^-\gamma\gamma$. Hadronisation is modelled with JETSET [12] using parameters described in [21]. The cluster fragmentation model in HERWIG is used to study the uncertainties due to quark and gluon jet fragmentation. The Monte Carlo samples pass through a detailed simulation of the OPAL detector [22] and are subjected to the same analysis procedure as applied to the data.

3. Analysis

The search described in this Letter addresses the Higgsstrahlung process $e^+e^- \rightarrow hZ$. The neutral Higgs boson h is assumed to decay into quark pairs of arbitrary flavour or into gluon pairs. The following hZ final states (search channels) are therefore considered, depending on the decay of the Z boson: the four-jet channel ($Z \rightarrow q\bar{q}$), the missing energy channel ($Z \rightarrow \nu\bar{\nu}$) and the electron, muon and tau channels ($Z \rightarrow e^+e^-, \mu^+\mu^-$ and $\tau^+\tau^-$).

The analysis assumes that the decay width of the Higgs boson is within the range $10^{-4} < \Gamma_h < 1 \text{ GeV}/c^2$. This ensures that the decay of the Higgs boson occurs within about 1 mm of the e^+e^- interaction point and that the reconstructed Higgs boson mass has a width that is dominated by the experimen-

Table 1

Number of events selected in the different search channels after consecutive cuts. In each case, the final likelihood cut is denoted by \mathcal{L} . The number of events found in the data is compared to the expectation from simulations. In the four-jet channel the numbers up to and including cut (8) are valid for all test-masses; those for cut (9) and the final likelihood cut are given for a test-mass of $100 \text{ GeV}/c^2$. The last two columns show the evolution of the selection efficiencies for Higgs bosons of 90 and $100 \text{ GeV}/c^2$ mass decaying exclusively into hadronic final states at 196 and 206 GeV centre-of-mass energy, respectively

Cut	Data	Total bkg.	$q\bar{q}(\gamma)$	4-fermi.	Efficiency in %	
					90 GeV/ c^2	100 GeV/ c^2
<i>Four-jet channel luminosity = 424.3 pb⁻¹</i>						
(1)	39090	38831.1	29929.3	8322.0	100	100
(2)	13692	13648.5	8602.5	5012.2	100	100
(3)	4645	4504.3	1077.9	3418.4	93	95
(4)	4200	4038.4	932.7	3105.7	92	94
(5)	3695	3561.3	603.2	2958.1	90	91
(6)	3594	3447.2	581.2	2866.0	89	90
(7)	2535	2399.6	504.2	1895.4	81	83
(8)	2081	1975.3	477.2	1498.1	78	80
(9)	659	637.4	155.8	481.6	59	66
\mathcal{L}	439	414.0	103.8	136.0	52	54
<i>Missing-energy channel luminosity = 420.9 pb⁻¹</i>						
(1)	9040	8524.6	6063.7	2382.4	87	78
(2)	2615	2391.3	686.0	1691.2	80	73
(3)	2462	2289.9	665.4	1614.6	77	73
(4)	1635	1598.4	110.7	1487.7	72	69
(5)	650	605.4	48.5	556.8	70	67
(6)	298	291.4	42.3	249.1	65	62
\mathcal{L}	123	133.1	6.3	126.6	45	48
<i>Electron channel luminosity = 422.3 pb⁻¹</i>						
(1)	18042	18221.3	12176.4	6045.0	92	97
(2)	558	538.7	252.8	286.1	75	78
(3)	429	378.6	171.0	207.6	74	78
\mathcal{L}	23	16.6	0.2	16.3	59	59
<i>Muon channel luminosity = 421.4 pb⁻¹</i>						
(1)	18008	18184.6	8715.5	9469.0	88	92
(2)	505	477.5	236.5	241.0	77	81
(3)	79	66.1	32.6	33.6	74	75
\mathcal{L}	16	15	6.6	8.4	64.8	62.4
<i>Tau channel luminosity = 409.0 pb⁻¹</i>						
(1)	10417	10082	5520.1	4561.8	83	78
(2)	1652	1687.6	187.0	1500.9	62	61
(3)	418	404.5	99.5	305.2	48	47
(4)	358	343.1	96.6	246.3	47	47
\mathcal{L}	3	8.8	0.23	8.57	27	21

tal resolution, between 2 and $5 \text{ GeV}/c^2$, depending on the search channel. The search strategies are similar to those applied by OPAL in the search for the SM Higgs boson [23] (see Ref. [24] for the missing energy channel) except that the b-tagging require-

ments are replaced by more elaborate kinematic selections.

In the searches addressing each of the final states, a preselection is applied first which strongly reduces the background while maintaining a high signal detec-

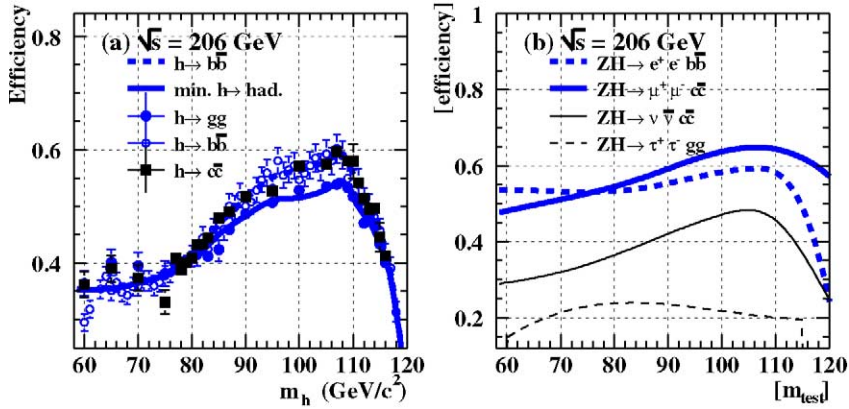


Fig. 1. Selection efficiencies for the Higgsstrahlung process in the different search channels, at $\sqrt{s} = 206$ GeV. (a) Four-jet channel, flavour-dependence. The full line shows the result from a spline fit to the points with the lowest efficiency. (b) All but the four-jet channel. In each case, the lowest of the efficiencies over all hadron flavours is plotted.

tion efficiency. The preselected events are then submitted to a likelihood test, which discriminates between the signal and the two most important background sources, 2-fermion and 4-fermion processes. Other background processes, in particular 2-photon events, are negligible after the first preselection cuts (see [23, Section 3]). The likelihood function is constructed from reference distributions of a number of discriminating variables which are obtained from detailed simulations of the signal and background processes. In the four-jet channel, these distributions are obtained from a three-dimensional spline fit to the distributions of simulated events where the dimensions are \sqrt{s} , the hypothetical Higgs boson mass (test-mass) and the variable itself.

Finally, a cut is applied on the value of this likelihood function. The cuts are chosen to optimise the signal efficiency over the statistical error on the background. For each of the search channels, the effect of the preselection and likelihood cuts on the data samples, the total background and its contributions, and on the signal detection efficiency for two test-masses can be followed through Table 1.

The signal efficiency is evaluated separately for each of the $h \rightarrow b\bar{b}$, $c\bar{c}$, $s\bar{s}$ and gg decay hypotheses. In these cases efficiencies were expected to be lower than for $h \rightarrow u\bar{u}$ and $d\bar{d}$ due to the presence of semileptonic decays, and the broader jets resulting from gluons or from the higher mass of the initial quarks. This has been verified using $e^+e^- \rightarrow ZZ$ events. At a given

test-mass, these efficiencies typically vary by about $\pm 5\%$. This is illustrated in Fig. 1(a) for the search in the four-jet channel. In deriving flavour independent bounds on the hZ coupling, the smallest of these efficiencies is used; it is obtained for $h \rightarrow gg$ in the four-jet and tau channels and for $h \rightarrow c\bar{c}$ or $b\bar{b}$ in the missing energy and lepton channels. These minimal efficiencies are shown for all but the four-jet search by the curves in Fig. 1(b).

3.1. Search in the four-jet channel

In the four-jet channel the main background arises from the $e^+e^- \rightarrow WW$ process. Further contributions are from $e^+e^- \rightarrow (Z/\gamma)^* \rightarrow q\bar{q}$ and $e^+e^- \rightarrow ZZ$. The analysis described below is repeated for fixed test-masses, in steps of $250 \text{ MeV}/c^2$, between 60 and $120 \text{ GeV}/c^2$. The following preselection is applied:

- (1) Events must be identified as multihadronic final states [25].
- (2) The effective centre-of-mass energy $\sqrt{s'}$ (disregarding initial-state photon radiation, see Ref. [25]), is required to exceed 80% of the total centre-of-mass energy.
- (3) Events are forced into four jets using the Durham algorithm [26] and are selected if the resolution parameter y_{34} is larger than 3×10^{-3} .

- (4) Each of the jets must contain at least two charged particle tracks to suppress events with isolated leptons or photons, like $e^+e^- \rightarrow q\bar{q}\ell^+\ell^-$.
- (5) The matrix element ME_{QCD} for the QCD-induced processes $e^+e^- \rightarrow q\bar{q}q\bar{q}$ and $e^+e^- \rightarrow q\bar{q}gg$ is calculated [27], approximating the parton momenta by the reconstructed jet momenta. The matrix element averaged over all possible flavour combinations is required to be within the range $-3 < \ln |ME_{QCD}| < -1$.
- (6) The χ^2 -probability resulting from a four-constraint (4C) kinematic fit which imposes energy and momentum conservation is required to be larger than 10^{-6} .
- (7) The four-fermion background is reduced by a cut on the matrix element ME_{4f} of the process $e^+e^- \rightarrow q\bar{q}q\bar{q}$, calculated using EXCALIBUR [15]. In the calculation the parton momenta are approximated by the jet momenta resulting from the 4C fit and the matrix element is averaged over all flavour combinations. Its value is required to be within the range $-8.5 < \ln |ME_{4f}| < -4.9$.
- (8) The $WW \rightarrow$ hadrons hypothesis is tested in a kinematic 6C fit imposing energy and momentum conservation and where the invariant masses of the two jet pairs are constrained to the W boson mass. To suppress the WW background, the largest of the χ^2 -probabilities, $P^{\max}(WW)$, for the three possible jet pairings is required to be less than 6.3%.
- (9) Finally, for each value of the test-mass, a kinematic fit is performed imposing energy and momentum conservation and constraining one dijet mass to the test-mass and the other to the Z boson mass. In the fit, the reconstructed Z boson mass is allowed to vary within its natural width according to a Gaussian distribution.²⁷ The largest of the χ^2 -probabilities $P^{\max}(Zh)$ resulting from the six possible jet assignments to the Z and the h bosons is required to exceed 10^{-6} .

The signal likelihood is constructed using the following 6 variables: (1) the maximum probability $P^{\max}(hZ)$ of the hZ kinematic fit; (2) the Higgsstrahlung matrix

element ME_{hZ} [28] for the test-mass considered and for the jet combination which yields $P^{\max}(hZ)$; the ratios (3) ME_{hZ}/ME_{4f} and (4) ME_{hZ}/ME_{QCD} ; (5) the difference between the maximum and minimum energies of the four jets after the 4C kinematic fit; and (6) $P^{\max}(WW)$. Distributions of these input variables are presented in Fig. 2, while the likelihood distributions for two test-masses are shown in Fig. 3(a) and (b). Events with a likelihood larger than 0.1 are accepted.

The signal efficiency and residual background rates are affected by the following systematic uncertainties: (a) uncertainties in modelling of the momenta, the angular and energy resolutions and the energy scale of the reconstructed jets are less than 2% for both the signal efficiency and the background rate. They have been determined by comparing calibration data taken at the Z resonance to the Monte Carlo simulation and transferring the observed differences to the simulation of the high energy data. (b) Uncertainties in modelling the preselection and likelihood variables are less than 3% for the signal and 4–9% for the background, depending on the test-mass. Weights were applied to the simulated events such that a $\chi^2 < 1$ is obtained when comparing the shapes of the distributions from the data and the simulation of the background (for each variable separately). The difference of the signal efficiency and background of the weighted and unweighted events is considered as the systematic error. It has been explicitly checked that a hypothetical signal is not hidden by this procedure. (c) Using alternatively JETSET and HERWIG to simulate hadron fragmentation yields a difference of 2–13% for the background. (d) The cross-section of the four-fermion processes, which dominates the residual background, is known to within 2% [30]. (e) Monte Carlo statistics contribute 1–5% for the signal and less than 3% for the background. Combining all these effects, the total systematic uncertainty amounts to less than 6% for the signal efficiency and 5–16% for the residual background.

The number of selected events in the four-jet channel with a likelihood value larger than 0.5 is shown in Fig. 4 (a) for test-masses between 60 and 120 GeV/c^2 . The selected data samples for mass hypotheses which differ by less than the mass resolution (of about 5 GeV/c^2 at high likelihood values) are strongly correlated. For a test-mass of 100 GeV/c^2 , 439 candi-

²⁷ The sensitivity of the search would be slightly lower if a Breit-Wigner distribution were used.

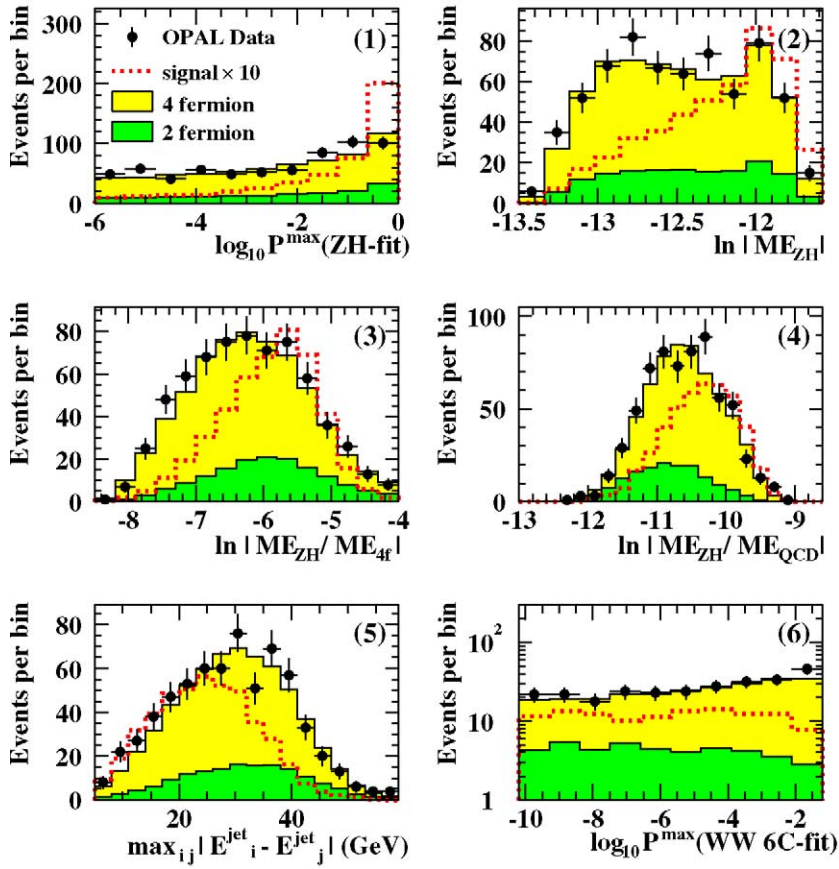


Fig. 2. Distributions of discriminating variables which have been used in the construction of the signal likelihood in the four-jet channel, the test-mass m_h being fixed at $100 \text{ GeV}/c^2$. The dots with error bars show the data. The light and dark shaded histograms show the expected background from four- and two-fermion processes. The dashed histograms show the signal, scaled by a factor ten, expected for a Higgs boson of $100 \text{ GeV}/c^2$ mass, with hZ coupling predicted by the SM and decaying only into hadronic final states

dates pass the final likelihood cut of 0.1 while 414 ± 53 events are expected from background processes and 40 events would be expected from Higgsstrahlung if the hZ coupling predicted by the SM is assumed and the Higgs boson decays only into hadronic final states. The signal to background ratio becomes more favourable for larger likelihood values.

3.2. Search in the missing energy channel

Signal events in the missing energy channel are characterised by two hadronic jets and a missing mass consistent with the Z boson mass. The dominant backgrounds are four-fermion processes, in particular from the semileptonic decays $e^+e^- \rightarrow WW \rightarrow q\bar{q}\ell^\pm\nu$, and

the irreducible process $e^+e^- \rightarrow ZZ \rightarrow \nu\bar{\nu}q\bar{q}$. Further contributions are from events with particles escaping detection along the beam-pipe, for example, from Z boson decays accompanied by initial-state photons or the untagged two-photon process $e^+e^- \rightarrow e^+e^-q\bar{q}$. The following preselection is applied:

- (1) To reject non-hadronic events, at least 7 charged particle tracks are required. At least 20% of all tracks must be of good quality (a minimum number of hits are required along the track, see Ref. [8]); this is to reject badly measured events, mainly two-photon processes and beam-wall interactions. The total transverse momentum p_t and the visible mass m_{vis} must satisfy $5 \times p_t + m_{\text{vis}} >$

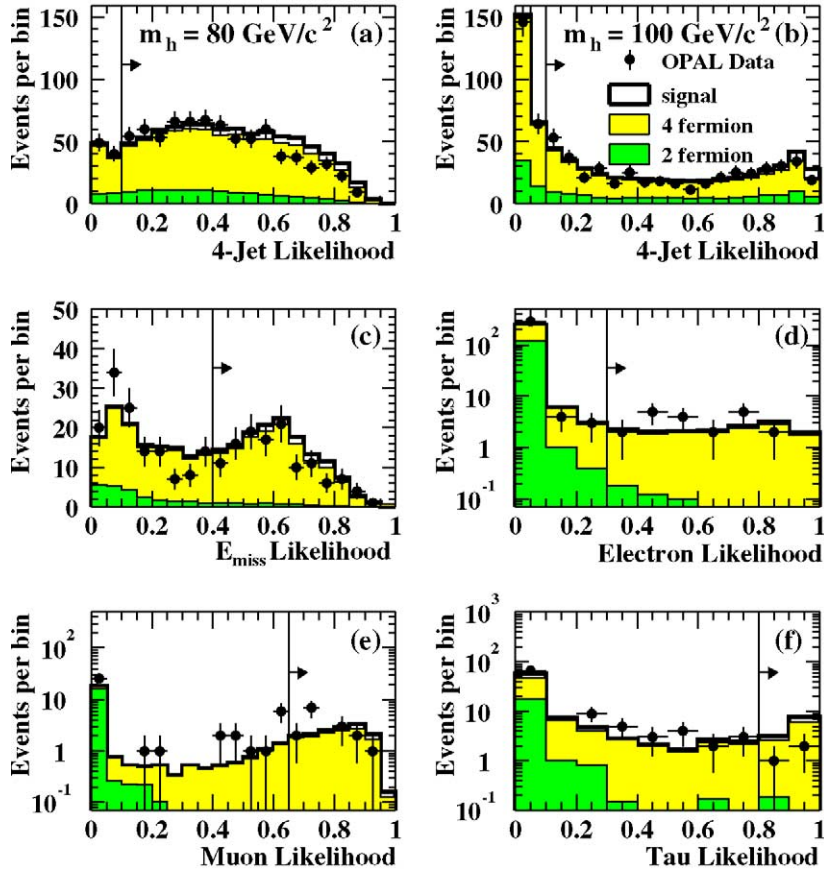


Fig. 3. Distributions of the signal likelihoods for the searches in the (a), (b) four-jet channel, (c) missing energy, (d) electron, (e) muon and (f) tau channels. In part (a) the test-mass m_h is fixed to $80 \text{ GeV}/c^2$; in all other parts it is $100 \text{ GeV}/c^2$. The points with error bars represent the data. The light and dark shaded histograms show the expected background from four- and two-fermion processes. The white histograms added on top of the background contributions show the signal expected for a Higgs boson of $100 \text{ GeV}/c^2$ mass ($80 \text{ GeV}/c^2$ in part (a)), with hZ coupling predicted by the SM and decaying only into hadronic final states. In each case, the vertical line indicates the final likelihood cut.

$\sqrt{s}/2$, and the visible energy $E_{\text{vis}} < 0.8\sqrt{s}$. The energy measured in the forward detector components [7], which cover small polar angles, must be $< 2 \text{ GeV}$ in the forward calorimeters, $< 5 \text{ GeV}$ in the gamma catcher and $< 5 \text{ GeV}$ in the silicon-tungsten calorimeter [32]. The overall energy observed in the region $|\cos\theta| > 0.9$, where θ denotes the polar angle with respect to the electron beam, must not exceed 20% of E_{vis} .

- (2) The missing momentum vector has to point to sensitive parts of the detector, $|\cos\theta_{\text{miss}}| < 0.95$, and the visible momentum must not have a large component along the beam axis, $|p_{\text{vis}}^z| < \sqrt{s}/5$.
- (3) The tracks and clusters in each event are forced into two jets using the Durham algorithm. Events

with partially contained jets are rejected by the requirement $|\cos\theta_{\text{jet}}| < 0.95$ imposed on each jet.

- (4) $(Z/\gamma)^* \rightarrow q\bar{q}$ events are suppressed by requesting $\phi_{\text{acop}} > 5^\circ$ where the acoplanarity angle ϕ_{acop} is the deviation of the angle between the two jets in the plane perpendicular to the beam axis from 180° .
- (5) The missing mass, m_{miss} , must be consistent with the Z boson mass: $50 \text{ GeV}/c^2 < m_{\text{miss}} < 130 \text{ GeV}/c^2$.
- (6) Identified semileptonic WW decays with energetic, isolated [32] leptons are discarded.

The signal likelihood function is constructed from 5 variables: (1) m_{miss} ; (2) $|\cos\theta_{\text{miss}}|$; (3) $\max|\cos\theta_{\text{jet}}|$,

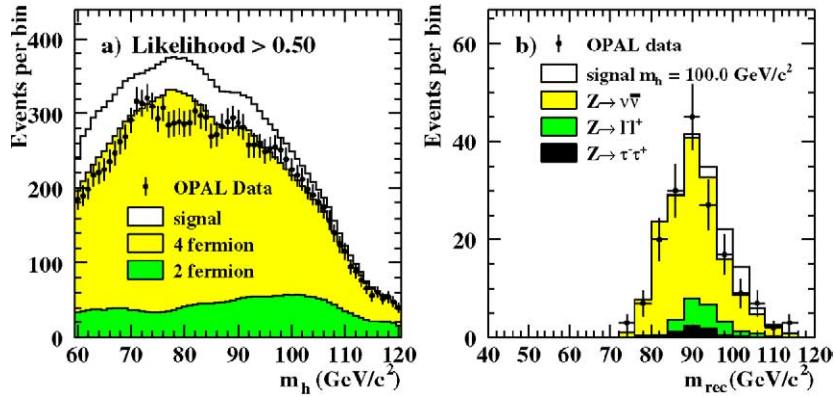


Fig. 4. (a) Number of candidates selected in the four-jet channel as a function of the test-mass m_h , together with the predicted backgrounds and the signal from Higgsstrahlung added on top of the background. For the purpose of this figure the likelihood cut is raised to 0.5. (b) Combined distributions of the reconstructed Higgs boson mass in the missing energy, electron, muon and tau channels. For the signal, the Higgs boson mass is fixed at $100 \text{ GeV}/c^2$. In both parts of the figure, the hZ coupling predicted by the SM and 100% hadronic Higgs boson decays are assumed.

i.e., the polar angle of the jet closest to the beam axis; (4) the χ^2 -probability $P(1C)$ of a one-constraint (1C) kinematic fit which imposes energy and momentum conservation and constrains the missing mass to the Z boson mass; (5) the angle between the missing momentum and the jet with the higher energy: $\cos \theta_{j\text{-miss}}$. The distributions of these discriminating variables are shown in Fig. 5 and the likelihood distribution in Fig. 3(c). Events with a likelihood larger than 0.4 are selected. The Higgs boson mass is reconstructed using the momenta provided by the 1C kinematic fit.

The number of events passing the likelihood selection is 123 (see Table 1) while 133 ± 11 events are expected from SM background processes. The most important systematic uncertainties [24] are from the modelling of the likelihood input variables and from the lepton isolation criteria. The signal efficiencies are affected by a total systematic error of 2.9%. The Monte Carlo estimates of the signal efficiencies were reduced by 2.5% to account for accidental vetoes due to accelerator-related backgrounds in the forward detectors. The reduction factor was determined from randomly triggered events.

3.3. Searches in the electron and muon channels

The signal events in the muon and electron channels are expected to have two energetic, oppositely charged, isolated leptons and two hadronic jets. The

dominant backgrounds are $e^+e^- \rightarrow (Z/\gamma)^*$ accompanied by initial state radiation and four-fermion processes, mainly from WW and ZZ pairs. The pre-selection is described in the following:

- (1) Events without hadronic jets are rejected by requiring at least 6 charged particle tracks. The visible energy E_{vis} must be larger than $0.6\sqrt{s}$ and the component of the total momentum along the beam axis must satisfy $|p_{\text{vis}}^z| < E_{\text{vis}} - 0.5\sqrt{s}$. This requirement reduces $e^+e^- \rightarrow (Z/\gamma)^*\gamma \rightarrow q\bar{q}\gamma$ and two-photon processes, $e^+e^- \rightarrow e^+e^-q\bar{q}$, significantly. All remaining events are forced into four jets using the Durham algorithm allowing isolated leptons to form low-multiplicity jets. Events are considered further if the jet resolution parameter y_{34} is larger than 10^{-4} .
- (2) Two oppositely charged electron or muon candidates must be identified, with energies larger than 30 (20) GeV for the higher- (lower-)energy candidate. The energy of muon candidates is deduced from the momentum measurement in the central tracking chamber; for electron candidates the energy measured in the electromagnetic calorimeter is used. The algorithms to identify muons and electrons are described in [31] and [32], respectively.
- (3) The remaining part of the event, after the two lepton candidates are removed, is reconstructed as a two-jet event using the Durham algorithm. If the

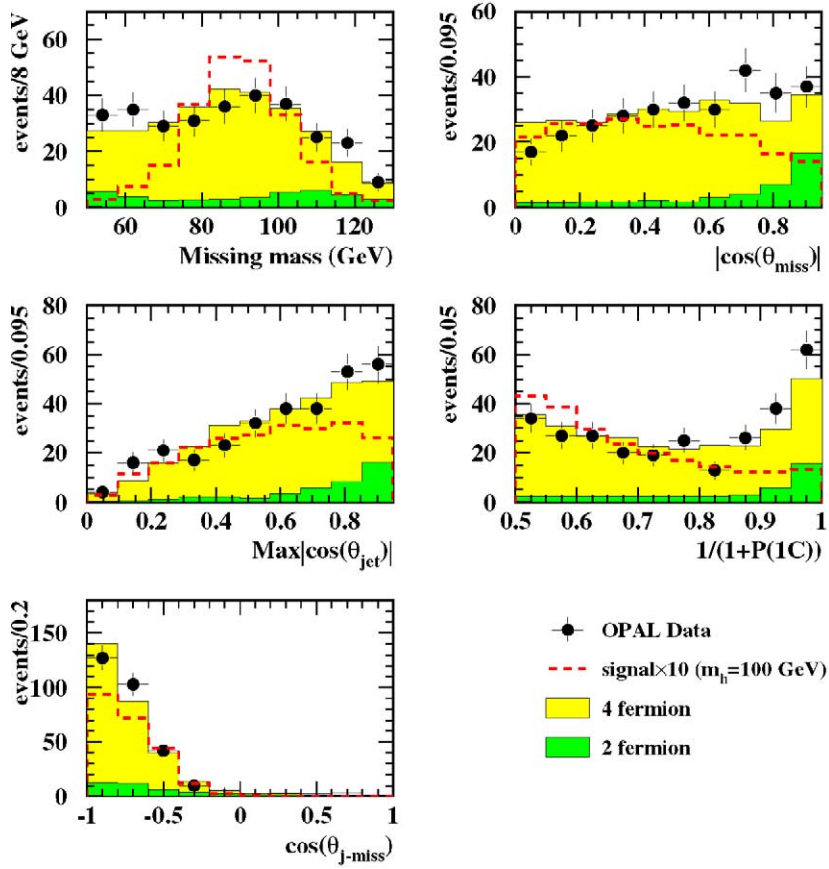


Fig. 5. Distributions of the discriminating variables used to calculate the signal likelihood in the missing energy channel. The light and dark shaded histograms show the expected background from four- and two-fermion processes. The dashed histograms show the signal, scaled by a factor ten, expected for a Higgs boson of $100 \text{ GeV}/c^2$ mass, with hZ coupling predicted by the SM and decaying only into hadronic final states.

lepton candidates are muons, a 4C kinematic fit requiring energy and momentum conservation is performed to improve the energy and mass resolution of the muon pair; the χ^2 -probability of the fit must exceed 10^{-5} . For both electron and muon candidate events, the invariant mass of the lepton pair is required to be larger than $40 \text{ GeV}/c^2$.

The signal likelihood is constructed from five variables in the muon channel and nine variables in the electron channel. Those in common are: (1) E_{vis}/\sqrt{s} ; (2) $\log_{10} y_{34}$; (3), (4) the measured transverse momenta of the two lepton candidates ordered by energy and calculated with respect to the nearest jet axis, used to discriminate against semileptonic charm or bottom decays; (5) the invariant mass of the lepton pair. For

each candidate in the electron channel, the additional variables are: (6), (7) $(E/p - 1)/\sigma$ for the two electron candidates, where the momentum p is measured in the central tracking detector, the energy E is measured using the calorimeter and σ denotes the total error in E/p ; (8), (9) the normalised ionisation energy losses in the central tracking chamber gas [24], for the two electron candidates. The event is selected if in the electron case the likelihood is larger than 0.3 or in the muon case larger than 0.65. Fig. 3(d) and (e) show the distribution of the two likelihood functions. The mass recoiling against the lepton pair is taken as the reconstructed Higgs boson mass.

The number of events passing the likelihood selection is 23 in the electron channel and 16 in the muon channel (see Table 1) while the corresponding

background expectations are 16.6 ± 5.1 and 15.0 ± 2.9 events. Systematic uncertainties [24] arise mainly from the fragmentation process, determined from a comparison of HERWIG and JETSET, and from different four-fermion rate predictions, given by grc4f, KORALW and EXCALIBUR. The signal efficiencies have total systematic errors of less than 2%.

3.4. Search in the tau channel

Signal events are expected to be composed of two hadronic jets from the Higgs boson decay, and two tau leptons from the Z decay. For each of the tau leptons, the decays into one or three charged particle tracks (“prongs”) are considered, possibly accompanied by calorimeter clusters from neutral particles. Important sources of background are the processes $e^+e^- \rightarrow ZZ^{(*)} \rightarrow q\bar{q}\ell^+\ell^-$, $e^+e^- \rightarrow WW \rightarrow q\bar{q}\ell^\pm\nu$ and $e^+e^- \rightarrow q\bar{q}(\gamma)$. The following preselection is applied:

- (1) Events must be identified as multihadronic final states [25]. The visible energy has to exceed $0.3\sqrt{s}$. In order to reject events in which particles escape detection close to the beam direction, the missing momentum vector is required to point to sensitive detector regions: $|\cos\theta_{\text{miss}}| < 0.95$. The scalar sum of the transverse momenta of all measured particles has to be larger than $45 \text{ GeV}/c$.
- (2) Two isolated tau lepton candidates, each with a momentum between 15 and $60 \text{ GeV}/c$, are required. These are identified with artificial neural networks (ANN) as described in [24]. Separate networks are developed for 1-prong and 3-prong decays. From the ANN output, the probability that a candidate is a real tau lepton is derived. The probabilities $P_{1,2}$ of the two tau candidates are combined to a two-tau-likelihood: $\mathcal{L}_{\tau\tau} = P_1 P_2 / (P_1 P_2 + (1 - P_1)(1 - P_2))$, which must exceed 0.1. If several tau pairs exist in the event, the pair with the largest $\mathcal{L}_{\tau\tau}$ is chosen.
- (3) After removing the two tau candidates, the rest of the event is grouped into two jets using the Durham algorithm. A kinematic fit (2C) is applied to the momenta of the two tau candidates and the two reconstructed jets, imposing energy and momentum conservation. The directions of the tau candidates are approximated by the visible momenta of their decay products; their energies are free parameters in the fit. The χ^2 -probability of the fit must be larger than 10^{-5} .
- (4) If both tau decays are classified as 1-prong decays, the momentum sum of both charged tracks must be less than $80 \text{ GeV}/c$; this is to reduce backgrounds from $e^+e^- \rightarrow ZZ \rightarrow q\bar{q}\mu^+\mu^-$ and $q\bar{q}e^+e^-$.

The signal likelihood is constructed using nine variables: (1) the visible energy; (2) $|\cos\theta_{\text{miss}}|$; (3) y_{34} obtained after reconstructing the event, including the tracks and clusters of the tau candidates, into four jets (the Durham algorithm is used); (4), (5) the angles between each of the two tau candidates and the nearest jet; (6) the energy of the most energetic muon or electron, if any; (7) the χ^2 -probability of a 3C kinematic fit, which in comparison to the 2C fit, in addition constrains the invariant mass of the two tau candidates to the Z boson mass; (8) the two-tau likelihood $\mathcal{L}_{\tau\tau}$; (9) the impact parameter joint probability of the tau candidate tracks calculated as in Ref. [29]. The resulting likelihood distribution is shown in Fig. 3(f). Events with a likelihood larger than 0.8 are accepted. The invariant mass of the two jets, resulting from the 3C-fit, is taken as the reconstructed Higgs boson mass.

Three events pass the likelihood cut (see Table 1) compared to 8.8 ± 1.5 events expected from background. The systematic errors are determined as described in [24]. The largest uncertainty arises from the purity of the tau lepton selection. The signal efficiencies are affected by a total systematic error of 15–17%.

4. Results

All search channels combined, 604 candidates are selected, while 588 ± 56 are expected from background processes (these numbers apply for a test-mass of $100 \text{ GeV}/c^2$ in the four-jet channel). Fig. 4(b) shows the distribution of the reconstructed Higgs boson mass for the candidates selected in the missing energy, electron, muon and tau channels, and for the corresponding expected backgrounds, added together.

No significant excess is observed in any of the search channels over the expected background from SM processes. In the following, an upper limit is set on the product of the cross-section σ_{hZ} of the Higgs

gsstrahlung process and the hadronic branching ratio $\text{Br}(h \rightarrow \text{hadrons})$ of the Higgs boson. For this purpose, these search results are combined with previous OPAL results, obtained at $\sqrt{s} = 91$ GeV in the missing energy, electron and muon channels [4], and at $\sqrt{s} = 189$ GeV in all channels [5].

The limits are obtained by using a weighted event counting method [33] which is briefly summarised below. The systematic errors are incorporated following Ref. [34]. A weight w_i is assigned to every candidate i , and the limit is calculated with respect to the observed sum of weights $W = \sum_i w_i$, which extends over all candidates in all search channels. The weights assigned to each candidate depend on the measured value of the search channel-dependent discriminating variable. They are chosen to optimise the discrimination power between the background (b) and signal plus background (s + b) hypotheses assuming the signal rate of a SM Higgs boson. For the optimisation and limit calculation, the probability density distributions to observe a weight sum W for the signal plus background and background only hypotheses, $\mathcal{P}(W; s + b)$ and $\mathcal{P}(W; b)$, respectively, are calculated. The calculation takes into account both the statistical and systematic uncertainties on the expected signal and background rates. The “optimal” weights are obtained by minimising the ratio:

$$\frac{\sigma(\mathcal{P}(W; s + b))}{|\langle W_{s+b} \rangle - \langle W_b \rangle|}, \quad (1)$$

where the numerator denotes the width of the probability density distribution $\mathcal{P}(W; s + b)$, and the denominator is the difference of the expectation values of W for the signal plus background and background only hypotheses. After optimisation, a candidate with a measured value of the discriminating variable, x , receives a large weight if the probability density to measure x for signal events is large compared to that for the background. Furthermore, the weights are reduced for candidates in regions with large systematic signal or background uncertainties.

A test-mass dependent 95% confidence level upper bound k_{95} is calculated for the quantity

$$k(m_h) = \frac{\sigma_{\text{hZ}}(m_h) \times \text{Br}(h \rightarrow \text{hadrons})}{\sigma_{\text{HZ}}^{\text{SM}}(m_h)},$$

where $\sigma_{\text{HZ}}^{\text{SM}}$ is the predicted SM cross-section for the Higgsstrahlung process. For each test-mass m_h the sig-

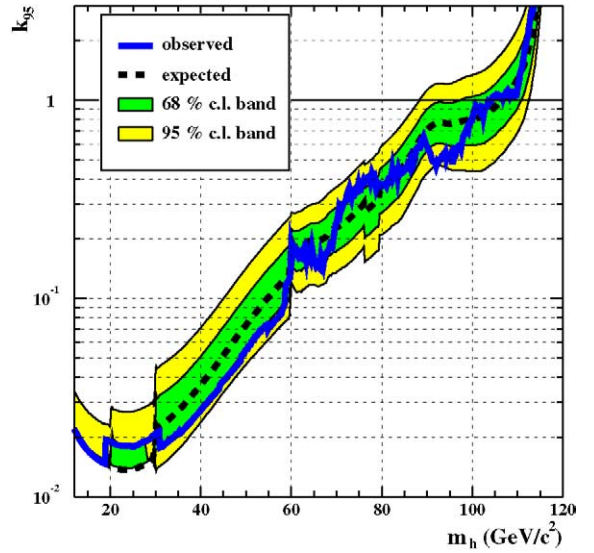


Fig. 6. The 95% confidence level upper bound on the product k of the Higgsstrahlung cross-section and the hadronic decay branching ratio of the Higgs boson, divided by the Higgsstrahlung cross-section in the SM. The thick solid line shows the observed limit. The limit expected on average, in a large number of simulated experiments, in the absence of a Higgsstrahlung signal is indicated by the dashed line while the dark- and light-shaded areas show the 68% and 95% probability bands around the average.

nal rate scaling factor k is adjusted until the probability to observe the sum W or a smaller value for the signal plus background hypothesis accounts for only 5% of the probability to observe W or a smaller value for the background only hypothesis:

$$\text{CL}_s(k_{95}) = \frac{\int_0^W d\xi \mathcal{P}(\xi, k_{95}; s + b)}{\int_0^W d\xi \mathcal{P}(\xi; b)} = 5\%. \quad (2)$$

Here $\mathcal{P}(\xi, k_{95}; s + b)$ denotes the probability density of a weight sum ξ for the signal plus background hypothesis which is calculated for a signal rate scaled by k_{95} .

This bound is shown in Fig. 6. In calculating this limit, the four-jet and tau channels were considered only for masses above 60 GeV/c^2 while the other channels contributed from 30 GeV/c^2 upwards. Between 12 and 30 GeV/c^2 , only the data taken in the vicinity of $\sqrt{s} = 91$ GeV are used [4]. The region below 12 GeV/c^2 is covered by a decay mode independent Higgs boson search conducted by OPAL [35].

Limits on the cross-section σ for arbitrary $\text{Br}(h \rightarrow \text{hadrons})$ or for arbitrary hZ coupling strength g_{hZ} can

be derived using the expression

$$\sigma_{95} = k_{95} \times \sigma_{\text{HZ}}^{\text{SM}} \times \text{Br}(h \rightarrow \text{hadrons}) \times (g_{\text{hZ}}/g_{\text{HZ}}^{\text{SM}})^2,$$

provided that the effective hZ coupling has the SM Lorentz structure.

Assuming the hZ coupling predicted by the SM, a Higgs boson decaying only into hadronic final states ($k_{95}(m_h) = 1$) is excluded for masses up to $104 \text{ GeV}/c^2$. For a Higgs boson also having the decay properties predicted by the SM, this limit is at $100 \text{ GeV}/c^2$.

5. Summary

A search has been performed for a hypothetical neutral scalar Higgs boson which is produced in Higgsstrahlung and which decays to hadrons of arbitrary flavour. The search is based on data collected by the OPAL experiment in e^+e^- collisions at centre-of-mass energies between 192 and 209 GeV. The results have been combined with earlier OPAL searches conducted at $\sqrt{s} \approx 91$ and $\sqrt{s} = 189$ GeV. No significant excess has been observed over the background expected from Standard Model processes. A mass-dependent upper bound is set, at the 95% confidence level, on the product of the Higgsstrahlung cross-section and the hadronic branching ratio of the Higgs boson. For a Higgs boson which couples to the Z boson with Standard Model strength and which decays exclusively into hadronic final states, a flavour independent lower bound of $104 \text{ GeV}/c^2$ is obtained on the mass.

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