



Measurement of the lifetime of the tau lepton

L3 Collaboration

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Abstract

The tau lepton lifetime is measured with the L3 detector at LEP using the complete data taken at centre-of-mass energies around the Z pole resulting in $\tau_\tau = 293.2 \pm 2.0(\text{stat}) \pm 1.5(\text{syst})\text{fs}$. The comparison of this result with the muon lifetime supports lepton universality of the weak charged current at the level of six per mille. Assuming lepton universality, the value of the strong coupling constant, α_s is found to be $\alpha_s(m_\tau^2) = 0.319 \pm 0.015(\text{exp}) \pm 0.014(\text{theory})$. © 2000 Elsevier Science B.V. All rights reserved.

1. Introduction

In the Standard Electroweak Model [1], the couplings of the leptonic charged and neutral currents to the gauge bosons are independent of the lepton generation. Measurements of the lifetime, τ_τ , and the leptonic branching fractions, $\mathcal{B}(\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau)$, of the tau lepton provide a test of this universality hypothe-

sis for the charged current. The leptonic width of the tau lepton [2],

$$\Gamma(\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau) \equiv \frac{\mathcal{B}(\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau)}{\tau_\tau} \quad (1)$$

$$= \frac{g_\tau^2 g_\ell^2}{m_W^4} \frac{m_\tau^5}{96(4\pi)^3} (1 + \epsilon_P) (1 + \epsilon_{\text{rad}}) (1 + \epsilon_{q^2}), \quad (2)$$

where $\ell = e, \mu$, depends on the coupling constants of the tau lepton and the lighter lepton to the W boson, g_τ and g_ℓ , respectively. Here m_τ and m_W are the masses of the tau lepton and the W boson. The quantities ϵ_P , ϵ_{rad} and ϵ_{q^2} are small corrections resulting from phase-space, radiation and the W propagator, respectively. For the decay of the muon, $\mu \rightarrow e \bar{\nu}_e \nu_\mu$, the same formula applies, with the muon mass and coupling, m_μ and g_μ , replacing those of the tau. The comparison of the tau lifetime and leptonic branching fractions with the muon lifetime gives a direct measurement of the ratios g_τ/g_e and g_τ/g_μ .

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Tau decays into hadrons are sensitive to the strong coupling constant, α_s , at the tau mass scale. Assuming universal coupling constants of the different lepton species to the W boson, the ratio of the hadronic width to the leptonic width, R_τ , can be expressed as:

$$R_\tau = \left(\frac{m_\mu}{m_\tau} \right)^5 \frac{\tau_\mu}{\tau_\tau} - C, \quad (3)$$

where $C = 1.9726$ contains the same corrections mentioned above.

R_τ is calculated in perturbative QCD [3–5]:

$$R_\tau = 3(|V_{ud}|^2 + |V_{us}|^2) S_{EW} \left(1 + \frac{\alpha_s}{\pi} + 5.2023 \left(\frac{\alpha_s}{\pi} \right)^2 + 26.366 \left(\frac{\alpha_s}{\pi} \right)^3 + (78 + d_3) \left(\frac{\alpha_s}{\pi} \right)^4 + \delta_{NP} \right). \quad (4)$$

The quantities $|V_{ud}|$ and $|V_{us}|$ are elements of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [6], S_{EW} [7] and δ_{NP} [4,8] describe electroweak radiative corrections and non-perturbative QCD contributions, respectively. The quantity d_3 is estimated as $d_3 = 27.5$ [5]. The perturbative theoretical uncertainty is taken to be $d_3 = 27.5 \pm 27.5$.

This paper presents a measurement of the tau lepton lifetime with the L3 detector at LEP, using data taken in 1995 at the Z pole. Furthermore, data from 1994 are re-analysed using an improved calibration and alignment of the central tracker. The lifetime is measured from the decay length in three-prong tau decays and from the impact parameter of one-prong tau decays⁹. The results are combined with our previously published analyses on data collected from 1990 to 1993 [9]. Previous measurements of the tau lepton lifetime have been reported by other experiments [10].

2. L3 detector

The L3 detector is described in Ref. [11]. This measurement is based primarily on the information

obtained from the central tracking system, which is composed of a Silicon Microvertex Detector (SMD) [12], a Time Expansion Chamber (TEC) and a Z-chamber. The SMD is made of two concentric layers of double-sided silicon detectors, placed at about 6 and 8 cm from the beam line. Each layer provides a two-dimensional position measurement, with a resolution of 7 and 14 μm for normally incident tracks, in the directions perpendicular and parallel to the beam direction, denoted as (x, y) and z coordinates, respectively. The TEC consists of two coaxial cylindrical drift chambers with 12 inner and 24 outer sectors. The sensitive region is between 10 and 45 cm in the radial direction, with 62 anode wires having a spatial resolution of approximately 50 μm in the plane perpendicular to the beam axis. The Z-chamber, which is situated just outside the TEC, provides a coordinate measurement along the beam axis direction.

3. Event sample

For this measurement data collected in 1994 and 1995 are used, which correspond to an integrated luminosity of 49 pb^{-1} and 31 pb^{-1} , respectively.

For efficiency and background estimates, Monte Carlo events are generated using the programs KORALZ [13] for $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ and $e^+e^- \rightarrow \tau^+\tau^-(\gamma)$, BHAGENE [14] for $e^+e^- \rightarrow e^+e^-(\gamma)$, DIAG36 [15] for $e^+e^- \rightarrow e^+e^-\text{ff}$, where ff is e^+e^- , $\mu^+\mu^-$, $\tau^+\tau^-$ or $q\bar{q}$, and JETSET [16] for $e^+e^- \rightarrow q\bar{q}(\gamma)$. The Monte Carlo events are passed through a full detector simulation based on the GEANT program [17], which takes into account the effects of energy loss, multiple scattering, showering and small time dependent detector inefficiencies. These events are reconstructed with the same program used for the data. The number of Monte Carlo events in each process is about ten times larger than the corresponding data sample.

Tau lepton pairs originating from Z decays are characterised by two low multiplicity, highly collimated jets in the detector. The selection of $e^+e^- \rightarrow \tau^+\tau^-(\gamma)$ events is described in detail in Ref. [18]; here only a general outline is given. In order to have high-quality reconstruction of the tracks, events are

⁹ An N -prong tau lepton decay indicates a decay with N charged particles in the final state.

accepted within a fiducial volume defined by $|\cos\theta_t| < 0.72$, where the polar angle θ_t is given by the thrust axis of the event with respect to the electron beam direction. The events must have at least two jets, and the number of tracks in each jet must be less than four. The background from $e^+e^- \rightarrow e^+e^-(\gamma)$ events is reduced by requiring the total energy deposited in the electromagnetic calorimeter to be less than 75% of the centre-of-mass energy. To reduce background from $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ the sum of the absolute momenta measured in the muon spectrometer must be less than 70% of the centre-of-mass energy. If muons are not reconstructed in the muon chambers they are identified by an energy deposit in the calorimeters which is characteristic of a minimum ionising particle. If this is the case for one jet, the opposite jet is required to exhibit a hadronic signature. This rejects dimuon as well as cosmic-ray events. The cosmic-ray background is further reduced by requiring a scintillation counter hit within 5 ns of the beam crossing. In addition, the distance of closest approach to the interaction point measured by the muon chambers must be less than two standard deviations of the resolution.

Following this procedure, 29679 and 13294 events are selected from the data collected in 1994 and 1995, respectively. The selection efficiency in the fiducial volume is estimated to be 76%. The purity of the tau pair sample is 98%.

4. Tracking

For this measurement a high quality of the track reconstruction is essential. A prerequisite is the control of the alignment between SMD and TEC and the drift time to drift distance calibration for the TEC. These calibrations, alignments and the estimation of resolution functions are performed with a clean sample of Bhabha and dimuon events, where tracks are known to originate from a common vertex. Particular effort is invested in the individual alignment of each sensor of the SMD and in the calibration of the boundaries of the TEC sectors. The procedure is described in detail in Ref. [19]. The performance of the track reconstruction is estimated from the dis-

tance between the two tracks at the vertex projected into the (x, y) plane. This quantity, called miss distance, is independent of the size and position of the e^+e^- interaction region. The distributions of miss distance for Bhabha and dimuon events collected during 1994 and 1995 are shown in Fig. 1. A Gaussian function is fitted to both distributions, from which an intrinsic resolution $\sigma_{\text{int}} = 33 \mu\text{m}$ and $31 \mu\text{m}$ is estimated for 1994 and 1995, respectively.

To guarantee good tracks for the analysis, the following cuts are made:

- Number of hits in the TEC ≥ 30 . This ensures a good curvature measurement.
- Number of SMD hits in the (x, y) plane ≥ 1 . This criterion selects tracks for which the error in the extrapolation to the vertex is well described by σ_{int} .
- Transverse momentum, $|p_t| \geq 500 \text{ MeV}$. Tracks with lower momenta have a larger uncertainty in the extrapolation to the vertex due to multiple Coulomb scattering in the SMD.
- Probability, $P(\chi^2)$, of the track fit larger than 1%. This requirement rejects bad fits.

5. Decay length method

For three-prong tau decays, the decay vertex of the tau is reconstructed and its distance to the centre of the interaction region is measured. The decay vertex is found from a minimisation with respect to the vertex coordinates (x_v, y_v) of the following χ^2 :

$$\chi^2 = \sum_{i=1}^{N_{\text{track}}} \left(\frac{\delta_i(x_v, y_v)}{\sigma_{\delta_i}} \right)^2. \quad (5)$$

In this equation, δ_i is the distance of closest approach of a track to the decay vertex coordinates. The error, σ_{δ_i} , is the quadratic sum of the intrinsic resolution, σ_{int} , and the error due to multiple Coulomb scattering, $\sigma_{\text{ms}}(p)$. Fig. 2 shows the distribution of the confidence level, $P(\chi^2)$, of the fit. Decay vertices with $P(\chi^2) < 1\%$ contain in most cases tracks with wrongly matched SMD hits and are rejected. The remaining distribution is flat, indicating a good description of the errors.

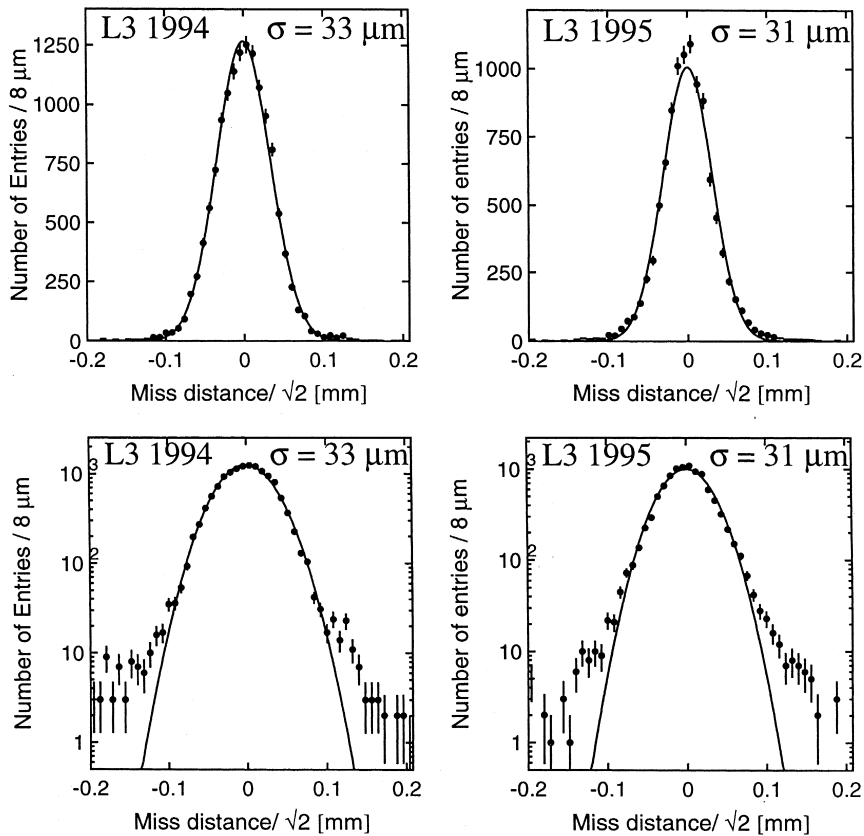


Fig. 1. Miss distance distributions from 1994 (left) and 1995 (right); Bhabha and dimuon events are shown in linear scale (upper) and logarithmic scale (lower). Dots are data and the solid line is the result of a fit with a Gaussian.

Fig. 3 shows the decay length distribution for the data collected in 1994 and 1995. Only decay length

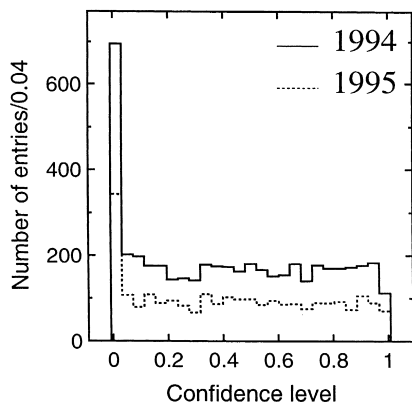


Fig. 2. Confidence level, $P(\chi^2)$, of the secondary vertex reconstruction.

values in the range $[-10, 20]$ mm with an error better than 5 mm are accepted for the lifetime determination. The number of selected decays is 4306 and 2314 for 1994 and 1995 data, respectively.

To obtain the average decay length, an unbinned maximum likelihood fit is applied to the observed decay length distribution. The likelihood function is calculated from a convolution of an exponential E , describing the tau decay time using the average decay length $\langle L \rangle$ as a parameter, with a Gaussian resolution function R . The likelihood function is written as:

$$\mathcal{L} = \prod_{i=1}^{N_{3p}} (1 - f_B) \cdot E \otimes R + f_B \cdot B. \quad (6)$$

In this equation the product runs over the accepted three-prong tau decays N_{3p} . The second term on the

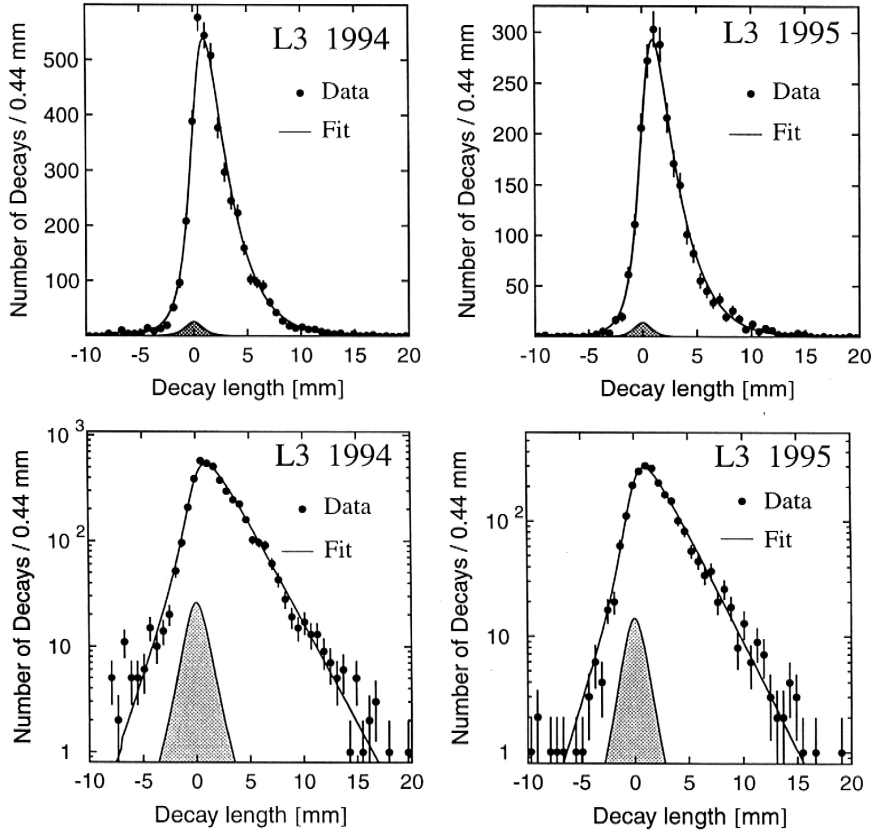


Fig. 3. Decay length distributions from 1994 (left) and 1995 (right); Three-prong tau decays are shown in linear scale (upper) and logarithmic scale (lower). The hatched areas represent the distributions of background events carrying no lifetime information.

right hand side has been added to take into account background carrying no τ lifetime information. The background fraction, f_B , is estimated from Monte Carlo and fixed in the fit. The likelihood function B is evaluated from the convolution of a Dirac delta function with the experimental resolution function.

The fit minimises $-\log \mathcal{L}$. Average decay lengths of $\langle L \rangle = (2.245 \pm 0.037)$ mm and $\langle L \rangle = (2.265 \pm 0.051)$ mm are determined for data from 1994 and 1995, respectively. The results of the fit are represented by the solid lines in Fig. 3.

The tau lifetime and average decay length are related through the following expression:

$$\tau_\tau = \frac{\langle L \rangle}{\beta \gamma c}. \quad (7)$$

Using this equation and taking into account the effects of radiation, lifetimes of $\tau_\tau = 292.5 \pm 4.9$ fs and $\tau_\tau = 295.2 \pm 6.6$ fs are obtained for the two data sets, where the errors are statistical only.

In order to check the decay length method, the analysis is repeated on a sample of Monte Carlo events. The difference between the input tau lifetime and the result of the fit is assigned as a systematic error due to the method. Systematic effects due to the non-ideal description of the resolution function are estimated from a one σ variation of its parameters. The deviation of the SMD radius from its nominal value is measured using Bhabha and dimuon events by minimising the track coordinate residuals from overlapping silicon sensors. Deviations of $(-5 \pm 5) \mu\text{m}$ and $(-3 \pm 5) \mu\text{m}$ are found in the data of 1994 and 1995, respectively. These results are com-

Table 1
Systematic errors for the decay length method

Error source (fs)	1994	1995
Method	0.5	0.5
Resolution function	1.5	2.0
SMD radius	0.7	0.7
Background estimate	0.8	0.6
Fit range	1.0	

patible with zero, and their uncertainties are translated into a systematic error on the lifetime. Uncertainties in the fraction of background events carrying no lifetime information are estimated from a $\pm 50\%$ variation of the fraction. Finally, the systematic error due to the fit range is estimated from the combined data by a 10% variation of their lower and upper bounds. This error also includes the effect of a variation of the cut on $P(\chi^2)$ between 0.1 and 1.5%. Table 1 summarises the systematic errors for the decay length method.

The lifetime measurements from the 6620 three-prong decays from 1994 and 1995 are combined. The systematic error due to the resolution function description is taken to be uncorrelated; for the other errors a 100% correlation is assumed. The result is $\tau_\tau = 292.9 \pm 3.9$ (stat) ± 1.9 (syst) fs.

6. Impact parameter method

A second measurement of the tau lifetime is obtained from the impact parameter in the plane perpendicular to the beam axis for one-prong tau decays. The impact parameter is the distance of closest approach, δ , of the track to the tau lepton production point, which is estimated by the beam position. In order to be sensitive to the lifetime, a sign is given to the impact parameter, according to the position of the intersection between the track and the tau direction of flight with respect to the beam position. The uncertainty on the impact parameter, σ_{ip} , is described as the quadratic sum of the intrinsic detector resolution, σ_{int} , the size of the interaction region, (σ_x, σ_y) , and a momentum dependent multiple Coulomb scattering contribution, $\sigma_{ms}(p)$,

$$\sigma_{ip}^2 = \sigma_{int}^2 + \sigma_x^2 \sin^2 \phi + \sigma_y^2 \cos^2 \phi + \sigma_{ms}^2(p), \quad (8)$$

where ϕ is the azimuthal angle in the plane perpendicular to the beam axis. The average values for the interaction region size are determined from Bhabha and dimuon data and listed in Table 2.

In contrast to the decay length method a more complicated function for the description of the tau decay is expected here, since for a one-prong tau decay the decay vertex is a priori not known. From a Monte Carlo study of the impact parameter distribution at generator level it is found that this function can be described in terms of three exponentials for positive and three exponentials for negative impact parameter values

$$U(\delta) = (1 - W) \sum_{i=1}^3 \frac{f_i^+}{\lambda_i^+} e^{-\frac{\delta}{\lambda_i^+}} + W \sum_{i=1}^3 \frac{f_i^-}{\lambda_i^-} e^{-\frac{\delta}{\lambda_i^-}}. \quad (9)$$

In this equation, W represents the fraction of negative impact parameter values, which originate from an imperfect reconstruction of the tau flight direction. The slopes of the exponentials, λ_i , contain the lifetime dependence of the distribution.

As for the decay length method, the lifetime is extracted from an unbinned maximum likelihood fit to the observed distribution. The likelihood is now determined from the convolution of a double Gaussian resolution function, which is obtained from Bhabha and dimuon samples, with the function of Eq. (9). The fit also accounts for background carrying no lifetime information.

Fig. 4 shows the impact parameter distributions from tau decays collected in 1994 and 1995. Impact parameters with a value in the range $[-0.9, 1.35]$ mm and an impact parameter error of less than $250 \mu\text{m}$ are accepted for the measurement. The fit yields a tau lifetime of $\tau_\tau = 292.7 \pm 3.3$ fs and $\tau_\tau = 295.0 \pm 4.9$ fs for the two data samples. The errors are statistical only.

Table 2
The size of the interaction regions

	σ_x (μm)	σ_y (μm)
1994	118 ± 1	14 ± 1
1995	148 ± 2	15 ± 3

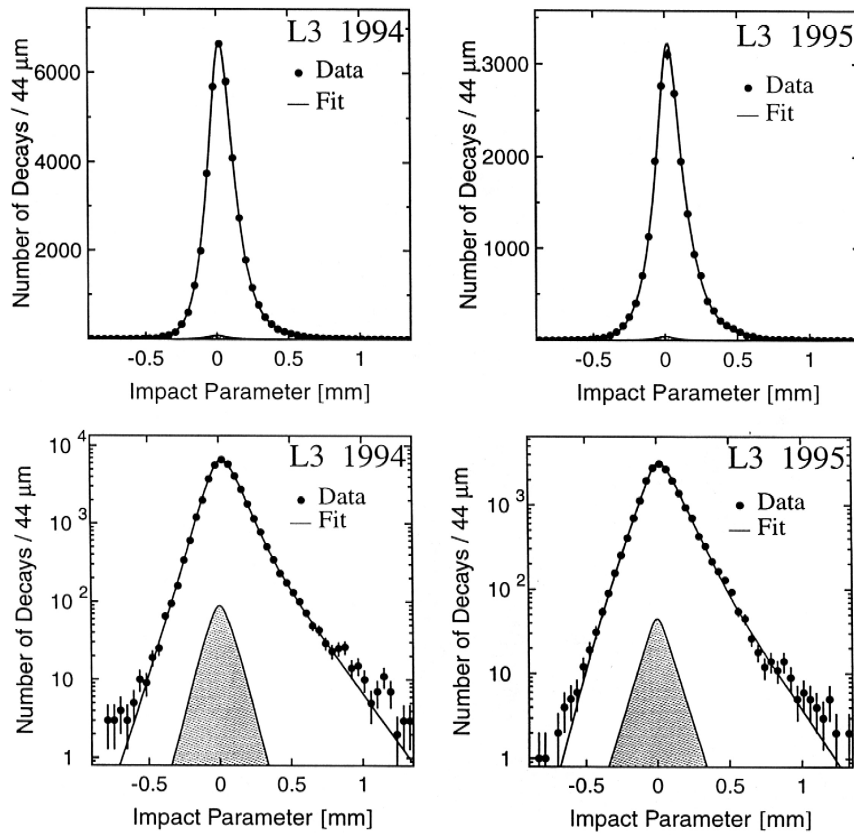


Fig. 4. Impact parameter distributions from 1994 (left) and 1995 (right); One-prong tau decays are shown in linear scale (upper) and logarithmic scale (lower). The hatched areas represent the distributions of background events which carry no lifetime information.

The method is checked on a Monte Carlo sample, from which the lifetime is determined in the same way as for the data. The difference between the input tau lifetime and the result of the fit is assigned as a systematic error due to the method. Systematic effects due to the uncertainty of the resolution function are estimated from a variation of its parameters according to their errors, with correlations taken into account. The beam spot size is varied according to its statistical errors. The change in the central value is assigned as a systematic uncertainty. The effect of the average SMD radial position uncertainty is treated in the same way as in the decay length analysis. The systematic effect due to the knowledge of the function $U(\delta)$ is evaluated by taking into account its statistical uncertainty and its dependence on the tau lifetime in the range from 250 to 350 fs. The uncertainty arising from the fraction of background events

is estimated from a $\pm 50\%$ variation of this fraction. The systematic error induced by the choice of the fit ranges is estimated from the combined data sample by a 10% variation of their bounds. Table 3 summarises the systematic errors for the impact parameter method.

Table 3
Systematic errors for the impact parameter method

Error source (fs)	1994	1995
Method	0.2	0.2
Resolution function	1.1	1.5
Beam spot size	0.5	0.5
SMD radius	0.7	0.7
Function $U(\delta)$	1.3	1.3
Background estimate	0.5	0.5
Fit range	0.5	

The lifetime measurements from the 58656 one-prong decays from 1994 and 1995 are combined. The systematic error due to the resolution function is taken to be uncorrelated. For the other errors a 100% correlation has been assumed. The result is $\tau_\tau = 292.8 \pm 2.7(\text{stat}) \pm 2.0(\text{syst})\text{ fs}$.

7. Discussion

The combination of the results obtained by the two methods with our previous ones [9] yields

$$\tau_\tau = 293.2 \pm 2.0(\text{stat}) \pm 1.5(\text{syst})\text{ fs}. \quad (10)$$

Correlations within the systematic errors are taken into account. This result supersedes all previous results [9,18]. This value is in good agreement with the current world average [20].

The measurements of the branching fractions, $\mathcal{B}(\tau \rightarrow e\bar{\nu}_e \nu_\tau) = (17.806 \pm 0.129)\%$ and $\mathcal{B}(\tau \rightarrow \mu\bar{\nu}_\mu \nu_\tau) = (17.341 \pm 0.129)\%$ [21] together with this lifetime measurement and the muon lifetime [20] yield $g_\tau/g_e = 0.996 \pm 0.006$ and $g_\tau/g_\mu = 0.996 \pm 0.006$ supporting the universality hypothesis.

From the tau lifetime, the tau mass, the muon mass and muon lifetime, R_τ is found to be $R_\tau = 3.595 \pm 0.048$. This corresponds to

$$\alpha_s(m_\tau^2) = 0.319 \pm 0.015(\text{exp}) \pm 0.014(\text{theory}). \quad (11)$$

The first error is due to the errors of the tau lifetime and the CKM matrix elements [20]. The second error is the quadratic sum of the uncertainties resulting from the renormalisation scale, the term fourth order in α_s , the electroweak corrections S_{EW} , and the non-perturbative correction, δ_{NP} . The renormalisation scale uncertainty is estimated following Ref. [22] by a variation between $0.4 \leq m_\tau^2/\mu^2 \leq 2.0$ and is the dominant contribution to the error. Other contributions to the theory error as discussed in Ref. [23] are not considered. This result is in good agreement with other measurements of α_s at the tau mass [24,20]. The value of $\alpha_s(m_\tau^2)$ is extrapolated to the Z mass using the renormalisation group equation [25] with the four loop calculation of the QCD β -func-

tions [26]. The result, $\alpha_s(m_Z^2) = 0.1185 \pm 0.0019(\text{exp}) \pm 0.0017(\text{theory})$, is in good agreement with the current world average value [20].

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