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Measurement of the $e^+e^- \rightarrow Z\gamma\gamma$ cross section and determination of quartic gauge boson couplings at LEP

L3 Collaboration

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Abstract

A first measurement of the cross section of the process $e^+e^- \rightarrow Z\gamma\gamma$ is reported using a total integrated luminosity of 231 pb⁻¹ collected with the L3 detector at centre-of-mass energies of 182.7 GeV and 188.7 GeV. By selecting hadronic events with two isolated photons the $e^+e^- \rightarrow Z\gamma\gamma$ cross section is measured to be $0.49^{+0.20}_{-0.17} \pm 0.04$ pb at 182.7 GeV and $0.47 \pm 0.10 \pm 0.04$ pb at 188.7 GeV. The measurements are consistent with Standard Model expectations. Limits on Quartic Gauge Boson Couplings a_0/Λ^2 and a_c/Λ^2 of $-0.009 \text{ GeV}^{-2} < a_0/\Lambda^2 < 0.008 \text{ GeV}^{-2}$ and $-0.007 \text{ GeV}^{-2} < a_c/\Lambda^2 < 0.013 \text{ GeV}^{-2}$ are derived at 95% confidence level. © 2000 Published by Elsevier Science B.V. All rights reserved.

1. Introduction

The LEP centre-of-mass energy (\sqrt{s}) for e^+e^- collisions has now exceeded the W pair and Z pair production thresholds, allowing the study of triple gauge boson production processes such as $e^+e^- \rightarrow Z\gamma\gamma$ and $e^+e^- \rightarrow W^+W^-\gamma$. Measurements of these processes give a new insight into the Standard Model of electroweak interactions (SM) [1–3]. The possibility of these triple gauge boson production processes proceeding via *s*-channel exchange of a fourth boson provides a probe of quartic gauge boson couplings (QGC). Such measurements were recently performed for the $e^+e^- \rightarrow W^+W^-\gamma$ process [4].

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Fig. 1. Three of the six SM diagrams contributing to $e^+e^- \rightarrow Z\gamma\gamma$ production. The other three SM diagrams are obtained by crossing the photon lines. A possible anomalous QGC diagram is also shown.

This letter describes the first measurement of the cross section of the process $e^+e^- \rightarrow Z\gamma\gamma$ followed by the hadronic decay of the Z. In the SM this process occurs by radiation of the photons from the incoming electron and/or positron, corresponding to a total of six diagrams, three of which are presented in Fig. 1. No QGC contribution is predicted at the tree level and $Z\gamma\gamma$ events are sensitive to anomalous QGC [5–7] contributions, as shown in Fig. 1.

The measurement uses data collected with the L3 detector [8–14] at LEP in 1997 and 1998 at average centre-of-mass energies of $\sqrt{s} = 182.7 \text{ GeV}$ and $\sqrt{s} = 188.7 \text{ GeV}$ corresponding to integrated luminosities of 55 pb⁻¹ and 176 pb⁻¹, respectively. These energies are respectively denoted as 183 GeV and 189 GeV hereafter.

The $e^+e^- \rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ signal is defined by three phase space cuts: photon energies above 5 GeV, photon angles with respect to the beam axis between 14° and 166° and invariant mass of the primary produced quarks, before any radiation, within a $\pm 2\Gamma_Z$ window around the Z mass, Γ_Z being the Z width. The KK2f Monte Carlo (MC) program [15] predicts signal cross sections of about 0.4 pb at both energies.

2. Event selection

The selection of events satisfying the signal definition given above is optimised using hadronic events generated at $\sqrt{s} = 189 \text{ GeV}$ with the KK2f MC program and at $\sqrt{s} = 183 \text{ GeV}$ with the PYTHIA 5.72 [16] MC program. Events from these MC programs failing the signal definition are termed QCD $\gamma\gamma$ background. Other background processes are generated both at $\sqrt{s} = 183 \text{ GeV}$ and $\sqrt{s} = 189 \text{ GeV}$ with the MC programs PYTHIA ($e^+e^- \rightarrow Ze^+e^-$ and $e^+e^- \rightarrow ZZ$), KORALZ4.02 [17] ($e^+e^- \rightarrow \tau^+\tau^-(\gamma)$), PHOJET 1.05c [18] ($e^+e^- \rightarrow e^+e^-q\bar{q}$) and KORALW 1.21 [19] for W⁺W⁻ production except for the $e\nu_eq\bar{q}'$ final states which are generated with EXCALIBUR [20]. Additional background sources are found to be negligible.

The L3 detector response is simulated using the GEANT 3.15 program [21], which takes into account the effects of energy loss, multiple scattering and showering in the detector. Time dependent detector inefficiencies, as measured in each data taking period, are reproduced in these simulations.

The selection of $e^+e^- \rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ candidates from balanced hadronic events with two photons and little energy deposition at low polar angles is based on photon energies and angles together with the invariant mass of the hadronic system. The photon energy and angle criteria follow directly from the signal definition whereas the invariant mass of the hadronic system is required to be between 74 GeV and 116 GeV. The main background after these selection requirements is due to the radiation of two initial state photons with a hadronic system failing the Z signal definition criteria. The boost β_Z of the recoiling system to the photons, assuming its mass to be the nominal Z mass, is on average larger for these background events. Candidate events are hence required to have $\beta_Z < 0.64$ at $\sqrt{s} = 183$ GeV and $\beta_Z < 0.66$ at $\sqrt{s} = 189$ GeV. Another class of background events is the so called radiative return to the Z, where a photon in the initial state is emitted, bringing the effective \sqrt{s} to the Z resonance. A Z boson is then produced decaying into a hadronic system with an electromagnetic energy deposition (e.g. final state radiation, misidentified electron or unresolved π^0) faking the least energetic photon of the signal selection. These events are rejected by an upper bound on the energy E_1^{γ} of the most energetic photon and a lower bound on the angle ω between the least energetic photon and its closest jet. Numerically $E_1^{\gamma} < 67.6$ GeV at $\sqrt{s} = 183$ GeV and $E_1^{\gamma} < 70.7$ GeV at $\sqrt{s} = 189$ GeV with $\omega > 17^{\circ}$ at both the energies.



Fig. 2. Distributions of (a) the invariant mass $M_{q\bar{q}}$ of the hadronic system, (b) the boost β_Z of the reconstructed Z boson, (c) the energy E_1^γ of the most energetic photon and (d) the angle ω between the least energetic photon and the nearest jet. Data, $Z\gamma\gamma$ and background MC are displayed for $\sqrt{s} = 189$ GeV. The arrows show the position of the final selection requirements. All the other selection criteria are applied for each plot.

Table 1

Yields of the $e^+e^- \rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ selection at $\sqrt{s} = 183 \,\text{GeV}$ and $\sqrt{s} = 189 \,\text{GeV}$. The signal efficiencies ε and the number of expected events for data and MC are given

	\sqrt{s} (GeV)		
	183	189	
ε	0.49	0.51	
Data	12	36	
MC	13.4	39.2	
Ζγγ	10.6	32.6	
QCDγγ	2.7	6.0	
Other	0.1	0.6	

Data and MC distributions of the selection variables are presented in Fig. 2 for $\sqrt{s} = 189 \text{ GeV}$, where selection criteria on all the other variables are applied. A good agreement between data and MC is observed.

3. Results and systematic uncertainties

The application of the selection procedure described above yields the signal efficiencies and selected data and MC events summarised in Table 1. A clear signal structure is observed in the recoil mass spectra of the two photons, presented in Fig. 3 for the two centre-of-mass energies under study. The $e^+e^- \rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ cross section at $\sqrt{s} = 183 \text{ GeV}$ and $\sqrt{s} = 189 \text{ GeV}$ is then determined from the number of events selected and the efficiency and background estimates from MC.

Systematic uncertainties on the cross section measurements are listed in Table 2. They include uncertainties arising from the signal MC statistical error of 3% at $\sqrt{s} = 183 \text{ GeV}$ and 5% at $\sqrt{s} = 189 \text{ GeV}$. The uncertainty on the accepted background due to MC statistics are 7% and 17% at $\sqrt{s} = 183 \text{ GeV}$ and $\sqrt{s} = 189 \text{ GeV}$, respectively. The calorimeter energy scale uncertainty is estimated by varying electromagnetic energies by



Fig. 3. Recoil mass to the photon pairs at (a) $\sqrt{s} = 183 \,\text{GeV}$ and (b) $\sqrt{s} = 189 \,\text{GeV}$ in data, $Z\gamma\gamma$ and background MC.

Table 2

Systematic uncertainties $\Delta \sigma$ on the e⁺e⁻ $\rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ cross section at $\sqrt{s} = 183 \text{ GeV}$ and $\sqrt{s} = 189 \text{ GeV}$

Source of systematics	$\Delta\sigma$ (pb)		
	183 GeV	189 GeV	
MC statistics	0.02	0.02	
energy scale	0.02	0.02	
selection procedure	0.01	0.01	
background normalisation	0.01	< 0.01	
reweighting procedure	0.01	_	
total	0.03	0.03	

 \pm 1% and hadronic energies by \pm 2%. Selection procedure systematics are obtained from the effect of removing each of the selection criteria. From a comparison of the KK2f and PYTHIA cross sections for hadronic events with a hard photon, a \pm 15% uncertainty on the background normalisation is conservatively estimated and propagated to the measured cross section. Uncertainties on signal efficiencies are estimated by comparing KK2f with PYTHIA and GRACE [22] MC program predictions and are found to be negligible. As these MC programs treat radiation with different approaches, these procedures also cover uncertainties in initial and final state radiation. The systematic error assigned to the reweighting procedure at $\sqrt{s} = 183$ GeV is estimated by applying the procedure to a sample generated with PYTHIA at $\sqrt{s} = 189$ GeV and comparing the corresponding cross section result to the previous one.



Fig. 4. Evolution of the $e^+e^- \rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ cross section with the centre-of-mass energy. Signal definition cuts described in the text are applied. The width of the band corresponds to the error that arises from MC statistics and theory uncertainty, estimated to be 1.5%. Dashed and dotted lines represent QGC predictions.

The cross section results are:

$$\sigma_{e^+e^- \to Z\gamma\gamma \to q\bar{q}\gamma\gamma}(183 \,\text{GeV}) = 0.34^{+0.14}_{-0.12} \pm 0.03 \,\text{pb} \quad (\text{SM } 0.396 \pm 0.005 \,\text{pb}),$$

$$\sigma_{e^+e^- \to Z\gamma\gamma \to q\bar{q}\gamma\gamma}(189 \,\text{GeV}) = 0.33 \pm 0.07 \pm 0.03 \,\text{pb} \quad (\text{SM } 0.365 \pm 0.003 \,\text{pb}),$$

where the first uncertainties are statistical and the second systematic. The values in parentheses denote the SM expectations calculated from the KK2f MC with its default set of input parameters. The error on the predictions is the quadratic sum of the MC statistical error and the theory uncertainty estimated as suggested in Ref. [15]. The measurements are in good agreement with these predictions. These results are also presented in Fig. 4 together with the expected evolution with \sqrt{s} of the SM cross section.

Scaling the measured cross sections for the Z hadronic branching ratio gives the $e^+e^- \rightarrow Z\gamma\gamma$ cross section at $\sqrt{s} = 183 \text{ GeV}$ and $\sqrt{s} = 189 \text{ GeV}$:

$$\sigma_{e^+e^- \to Z\gamma\gamma}(183 \,\text{GeV}) = 0.49^{+0.20}_{-0.17} \pm 0.04 \,\text{pb},$$

$$\sigma_{e^+e^- \to Z\gamma\gamma}(189 \,\text{GeV}) = 0.47 \pm 0.10 \pm 0.04 \,\text{pb}$$

4. Limits on quartic gauge boson couplings

Anomalous QGC contributions to $Z\gamma\gamma$ production via the *s*-channel exchange of a Z are described by two additional terms of dimension six in the Lagrangian [5]:

$$\mathscr{L}_6^0 = -\frac{\pi\alpha}{4\Lambda^2} a_0 F_{\mu\nu} F^{\mu\nu} W_{\rho} \cdot W^{\rho}, \quad \mathscr{L}_6^c = -\frac{\pi\alpha}{4\Lambda^2} a_c F_{\mu\rho} F^{\mu\sigma} W^{\rho} \cdot W_{\sigma}$$

where α is the electromagnetic coupling, $F_{\mu\nu}$ is the field strength tensor of the photon and W_{μ} is the weak boson field. For $Z\gamma\gamma$ the third component of W_{μ} , $Z_{\mu}/\cos\theta_W$, is relevant. The parameters a_0 and a_c describe the strength of the QGC and Λ represents the scale of the New Physics responsible for the coupling. \mathscr{L}_6^0 and \mathscr{L}_6^c are separately C and P conserving and no CP violating operators contribute to the anomalous $ZZ\gamma\gamma$ vertex. A more detailed description of QGC has recently appeared [7]. While indirect limits on the QGC were derived from precision measurements at the Z pole [23], studies of $Z\gamma\gamma$ and $W^+W^-\gamma$ production probe the quantities a_0/Λ^2 and a_c/Λ^2 in a direct way. The $e^+e^- \rightarrow Z\gamma\gamma$ process is expected to have higher sensitivities than $e^+e^- \rightarrow W^+W^-\gamma$. This is due to an extra factor of $1/\cos^4\theta_W$ in the QGC cross section, to the larger SM cross section and data statistics and to the smaller number of SM diagrams [6].

QGC are expected to manifest themselves via deviations in the total $e^+e^- \rightarrow Z\gamma\gamma$ cross section, as presented in Fig. 4. As the $Z\gamma\gamma$ production occurs in the SM via *t*-channel diagrams, the three body phase space favoured in the QGC mediated production is different, in particular resulting in a harder spectrum of the least energetic photon [7]. Fig. 5a and 5b compare these reconstructed spectra with the predictions from signal and background MC at $\sqrt{s} = 183 \text{ GeV}$ and $\sqrt{s} = 189 \text{ GeV}$. The expectations for an anomalous value of a_0/Λ^2 or a_c/Λ^2 are also shown. These QGC predictions are obtained by reweighting each SM signal MC event with the ratio $\mathscr{W}(\Omega, a_0/\Lambda^2, a_c/\Lambda^2)$, a function of its phase space Ω derived from the two photons and the Z mass and the values of the couplings:

$$\mathscr{W}\left(\Omega, a_0/\Lambda^2, a_c/\Lambda^2\right) = \frac{|\mathscr{M}_{\rm SM}(\Omega) + \mathscr{M}_{\rm QGC}\left(\Omega, a_0/\Lambda^2, a_c/\Lambda^2\right)|^2}{|\mathscr{M}_{\rm SM}(\Omega)|^2}.$$



Fig. 5. Energy E_2^{γ} of the least energetic photon for (a) $\sqrt{s} = 183 \,\text{GeV}$ and (b) $\sqrt{s} = 189 \,\text{GeV}$. Data, $Z\gamma\gamma$ and background MC are displayed together with QGC predictions.

 \mathcal{M}_{SM} denotes the SM matrix element and \mathcal{M}_{QGC} the QGC one, both calculated analytically [6]. Possible extra initial state photons are taken into account in the calculation of Ω .



Fig. 6. Two dimensional contours for the QGC parameters a_0 / Λ^2 and a_c / Λ^2 .

A simultaneous fit to the two energy spectra is performed leaving one of the two QGC free at a time, fixing the other to zero. The SM predictions in the fit procedure are reweighted as described above, yielding the 68% confidence level (CL) measurements:

$$a_0/\Lambda^2 = 0.001 \pm 0.004 \,\text{GeV}^{-2}$$
 and $a_c/\Lambda^2 = 0.003 \pm 0.005 \,\text{GeV}^{-2}$,

in agreement with the expected SM value of zero. A simultaneous fit to both the parameters yields the 95% CL limits:

$$-0.009 \,\text{GeV}^{-2} < a_0/\Lambda^2 < 0.008 \,\text{GeV}^{-2}$$
 and $-0.007 \,\text{GeV}^{-2} < a_0/\Lambda^2 < 0.013 \,\text{GeV}^{-2}$.

as shown in Fig. 6. A correlation of -35% is observed. The experimental systematic uncertainties and those on the SM $e^+e^- \rightarrow Z\gamma\gamma \rightarrow q\bar{q}\gamma\gamma$ cross section predictions are taken into account.

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